

5.1 Multiplying Powers with the Same Base (M2 10.1)

• Multiplying Powers

- You can use a property of exponents to multiply powers with the same base.
- A product of powers with the same base can be re-written using one exponent.

▪ Ex: $3^4 * 3^2 = (3 \cdot 3 \cdot 3 \cdot 3) \cdot (3 \cdot 3) = 3^6$

- In general, an the product of powers with the same base can be written using variables:

$$a^m * a^n = a^{m+n} \leftarrow \begin{array}{l} \text{add exponents} \\ \text{same base} \end{array}$$

- Ex: What is each expression written using each base only once?

• $12^4 * 12^3 = 12^{4+3} = 12^7$

• $(-5)^{-2}(-5)^7 = (-5)^{-2+7} = (-5)^5$

• Multiplying Powers in Algebraic Expressions

- When variable factors have more than one base, be careful to combine only those powers with the same base.
- Expressions should always be given with positive exponents.

$$xa^{-n} = \frac{x}{a^n} \leftarrow \begin{array}{l} \text{switch sign, put} \\ \text{term in denominator} \end{array}$$

- Ex: What is the simplified form of each expression?

• $4z^5 * 9z^{-12} = (4 \cdot 9)(z^5 \cdot z^{-12})$
 $= 36z^{5+(-12)} = 36z^{-7} = \frac{36}{z^7}$

• $2a^1 * 9a^4 * 3a^2 = (2 \cdot 9 \cdot 3)(a \cdot a^4 \cdot a^2)$
 $= 54a^{1+4+2} = 54a^7$

• Multiplying with Scientific Notation

- You can use the property for multiplying powers with the same base to multiply numbers written in scientific notation

- Scientific notation: $a * 10^b$ where $1 \leq |a| < 10$

- Ex: At 20°C, one cubic meter of water has a mass of about $9.98 * 10^5$ g. Each gram of water contains about $3.34 * 10^{22}$ molecules of water. About how many molecules of water does the droplet of water shown below contain?

$V = 1.13 \times 10^{-7} \text{ m}^3$

$$\begin{aligned} & (1.13 \cdot 10^{-7} \text{ m}^3) (9.98 \cdot 10^5 \text{ g/m}^3) (3.34 \cdot 10^{22} \text{ molec./g}) \\ & = (1.13 \cdot 9.98 \cdot 3.34) \cdot 10^{-7+5+22} \\ & = 37.7 \cdot 10^{20+1} = \boxed{3.77 \cdot 10^{21}} \end{aligned}$$

• Simplifying Expressions written with Rational Exponents

○ Exponents can also be expressed as fractions. Fractional exponents are called rational exponents.

○ Recall that $3^2 = 3 * 3 = 9$. You can write the same expression using rational exponents: $9^{\frac{1}{2}} = 3$

○ In general, $a^{\frac{1}{m}} = b$ means that b multiplied as a factor m times equals a.

▪ Ex: Simplify the expression $(2a^{\frac{2}{3}} * 3b^{\frac{1}{4}})(a^{\frac{1}{3}} * 5b^{\frac{1}{2}})$

$$= (2 \cdot 3 \cdot 5)(a^{\frac{2}{3}} \cdot a^{\frac{1}{3}})(b^{\frac{1}{4}} \cdot b^{\frac{1}{2}})$$

$$= 30 a^{\frac{3}{3}} b^{\frac{3}{4}}$$

$$= \boxed{30ab^{\frac{3}{4}}}$$

▪ Ex: Simplify the expression $(8b^{\frac{2}{3}} * 9t^{\frac{1}{5}})(8b^{\frac{5}{3}} * 9t^{\frac{3}{5}})$

$$(8 \cdot 9 \cdot 8 \cdot 9)(b^{\frac{2}{3}} \cdot b^{\frac{5}{3}})(t^{\frac{1}{5}} \cdot t^{\frac{3}{5}})$$

$$\boxed{5184 b^{\frac{7}{3}} t^{\frac{4}{5}}}$$

5.2 Power Rule (M2 10.2)

- Simplifying a Power Raised to a Power

- You can use properties of exponents to simplify a power raised to a power or a product raised to a power.

$$(x^5)^2 = x^5 * x^5 = x^{5+5} = x^{5*2} = x^{10}$$

- To raise a power to a power, multiply the exponents.

$$(a^m)^n = a^{mn}$$

where $a \neq 0$ and m and n are rational numbers

- Ex: Simplify

$$\bullet (5^4)^2 = 5^{4 \cdot 2} = \boxed{5^8}$$

$$\bullet \left(p^{\frac{2}{3}}\right)^{\frac{1}{2}} = p^{\frac{2}{3} \cdot \frac{1}{2}} = \boxed{p^{1/3}}$$

- Simplifying an Expression with Powers

- Use the order of operations when you simplify an exponential expression.

- Ex: What is the simplified form of $y^3(y^{\frac{5}{2}})^{-2}$ = $y^3 \cdot y^{-\frac{10}{2}}$

$$y^3 \cdot y^{-5} = y^{-2} = \boxed{\frac{1}{y^2}}$$

- Ex: What is the simplified form of $x^2(x^6)^{-4}$

$$x^2 \cdot x^{6 \cdot -4} = x^2 \cdot x^{-24} = x^{-22} = \boxed{\frac{1}{x^{22}}}$$

- Simplifying a Product Raised to a Power

- You can use repeated multiplication to simplify an expression like $(4m^{\frac{1}{2}})^3$.

$$\left(4m^{\frac{1}{2}}\right)^3 = 4m^{\frac{1}{2}} * 4m^{\frac{1}{2}} * 4m^{\frac{1}{2}}$$

$$= 4 * 4 * 4 * m^{\frac{1}{2}} * m^{\frac{1}{2}} * m^{\frac{1}{2}}$$

$$= 4^3 m^{\frac{3}{2}}$$

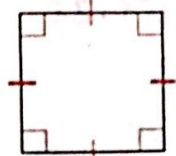
$$= 64m^{\frac{3}{2}}$$

- To raise a product to a power, raise each factor to the power and multiply.

where $a \neq 0$, $b \neq 0$, and m is a rational number

Ex: $(3x)^4 = 3^4 x^4 = \boxed{81x^4}$

- Ex: What is a simplified expression for the area of the square shown?



$5x^3$

$$A = (5x^3)^2 = 5^2 x^{3 \cdot 2}$$

$$= 5^2 x^6 = \boxed{25x^6}$$

- Simplifying an expression with Products

- What is the simplified form of $(n^{\frac{1}{2}})^{10} (4mn^{-\frac{2}{3}})^3$?

$$n^{10 \cdot \frac{1}{2}} \cdot 4^3 m^3 n^{-2}$$

$$= 4^3 m^3 n^5 n^{-2} = \boxed{64m^3 n^3}$$

- What is the simplified form of $(6ab)^3 (5a^{-3})^2$?

$$6^3 a^3 b^3 \cdot 5^2 a^{-6}$$

$$= 5^2 \cdot 6^3 \cdot a^3 \cdot a^{-6} \cdot b^3$$

$$= 25 \cdot 216 \cdot a^{-3} b^3$$

$$= 5400 a^{-3} b^3$$

$$= \boxed{\frac{5400b^3}{a^3}}$$

- Raising a Number in Scientific Notation to a Power

- You can use the property of raising a product to a power to solve problems involving scientific notation.

$$(a \cdot 10^m)^n = a^n \cdot 10^{mn}$$

- Ex: The expression $\frac{1}{2}mv^2$ gives the kinetic energy, in joules, of an object with a mass of m kg traveling at a speed of v meters per second. What is the kinetic energy of an experimental unmanned jet with a mass of $1.3 \cdot 10^3$ kg traveling at a speed of about $3.1 \cdot 10^3$ m/s?

$$m = 1.3 \times 10^3 \text{ kg}$$

$$v = 3.1 \times 10^3 \text{ m/s}$$

$$E = \frac{1}{2} (1.3 \times 10^3) (3.1 \times 10^3)^2$$

$$= \frac{1}{2} (1.3 \times 10^3) (3.1^2 \times 10^{3 \cdot 2})$$

$$= \left(\frac{1}{2} \cdot 1.3 \cdot 3.1^2 \right) \times 10^{3+6}$$

$$= \boxed{6.2 \times 10^9 \text{ J}}$$

5.3 Quotient Rule (M2 10.3)

- Dividing Algebraic Expressions

- You can use properties of exponents to divide powers with the

same base

- Shown with repeated multiplication:

$$\frac{4^5}{4^3} = \frac{4 * 4 * 4 * 4 * 4}{4 * 4 * 4} = 4^2$$

- To divide powers with the same base, subtract the exponents.

$$\frac{a^m}{a^n} = a^{m-n}$$

exp. of numerator
- exp. of denominator

where $a \neq 0$ and m and n are rational numbers

- Ex: What is the simplified form of each expression?

$$\frac{2^6}{2^2} = 2^{6-2} = \boxed{2^4}$$

$$\frac{y^{\frac{3}{4}}}{y^{\frac{1}{2}}} = y^{\frac{3}{4} - \frac{1}{2}} = y^{\frac{3}{4} - \frac{2}{4}} = \boxed{y^{\frac{1}{4}}}$$

$$\frac{x^4 y^{-1} z^8}{x^4 y^{-5} z} = x^{4-4} y^{-1-(-5)} z^{8-1} = x^0 y^4 z^7 = \boxed{y^4 z^7}$$

- Dividing Numbers in Scientific Notation

- The property of dividing powers can be used to divide numbers in scientific notation.

- Ex: Population density describes the number of people per unit area. During one year, the population of Angola was $1.21 * 10^7$ people. The area of Angola is $4.81 * 10^5$ mi². What was the population density of Angola that year?

$$\text{pop D} = \frac{1.21 * 10^7 \text{ people}}{4.81 * 10^5 \text{ mi}^2} = \frac{1.21}{4.81} * 10^{7-5} = 0.252 * 10^{2-1}$$

$$= 2.52 * 10^1 \text{ people/mi}^2$$

$$= \boxed{25.2 \text{ people/mi}^2}$$

• Raising a Quotient to a Power

- You can use repeated multiplication to simplify a quotient raised to a power.

$$\left(\frac{x}{y}\right)^3 = \frac{x}{y} * \frac{x}{y} * \frac{x}{y} = \frac{x * x * x}{y * y * y} = \frac{x^3}{y^3}$$

- To raise a quotient to a power, raise the numerator and the denominator to the power and simplify.

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

where $a \neq 0$, $b \neq 0$, and n is a rational number

- Ex: What is the simplified form of $\left(\frac{z^2}{5}\right)^3$?

$$= \frac{(z^2)^3}{5^3} = \boxed{\frac{z^6}{125}}$$

- Ex: What is the simplified form of $\left(\frac{a^3}{a^5}\right)^4$?

$$= \frac{(a^3)^4}{(a^5)^4} = \frac{a^{12}}{a^{20}} = a^{12-20} = a^{-8} = \boxed{\frac{1}{a^8}}$$

• Simplifying an Exponential Expression

- Recall that negative exponents Flip fractions.

$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$$

for all rational numbers a and b, and positive integers n.

- Ex: What is the simplified form of $\left(\frac{2x^6}{y^4}\right)^{-3}$?

$$= \left(\frac{y^4}{2x^6}\right)^3 = \frac{(y^4)^3}{(2x^6)^3} = \frac{y^{12}}{2^3 x^{18}} = \boxed{\frac{y^{12}}{8x^{18}}}$$

5.4 Simplifying Radicals (M1 5.8)

- Removing Perfect-Square Factors

- A radical expression is an expression that contains a radical.

- The radicand has no perfect-square factors other than 1.
 - The radicand contains no fractions
 - No radicals appear in the denominator of a fraction

- Simplified vs. Not Simplified Radicals

- Simplified: $3\sqrt{5}$ $9\sqrt{x}$ $\frac{\sqrt{2}}{4}$

- Not Simplified: $3\sqrt{12}$ $\sqrt{\frac{x}{2}}$ $\frac{5}{\sqrt{7}}$

- Multiplication Property of Square Roots

- For $a \geq 0$ and $b \geq 0$, $\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$
 - Can be used to simplify radicals by removing perfect-square factors.

- Ex: What is the simplified form of $\sqrt{160}$?

$$= \sqrt{16} \cdot \sqrt{10}$$

$$= \boxed{4\sqrt{10}}$$

- Ex: What is the simplified form of $\sqrt{72}$?

$$= \sqrt{9} \cdot \sqrt{8}$$

$$= 3\sqrt{4 \cdot 2} = 3\sqrt{4} \cdot \sqrt{2} = \boxed{6\sqrt{2}}$$

- Removing Variable Factors

- Sometimes, you can simplify radical expressions that contain variables
 - A variable with an even exponent is a perfect square. $\sqrt{n^6} = n^3$
 - A variable with an odd exponent is the product of a perfect square and the variable. (i.e. $n^3 = n^2 \cdot n$)

- Ex: What is the simplified form of $\sqrt{54n^7}$?

$$= \sqrt{9 \cdot 6 \cdot m^6 \cdot m}$$

$$= \sqrt{9m^6} \cdot \sqrt{6m} = \boxed{3m^3\sqrt{6m}}$$

- Ex: What is the simplified form of $-m\sqrt{80m^9}$?

$$= -m\sqrt{4m^8} \sqrt{20m}$$

$$= -m \cdot 2m^4 \sqrt{4 \cdot 5m} \rightarrow = -2m^5 \sqrt{4} \sqrt{5m}$$

$$= -2m^5 \cdot 2 \sqrt{5m}$$

$$= \boxed{-4m^5\sqrt{5m}}$$

- Multiplying Two Radical Expressions

- What is the simplified form of $2\sqrt{7t} \cdot 3\sqrt{14t^2}$?

$$= 2 \cdot 3 \cdot \sqrt{7t} \cdot \sqrt{14t^2}$$

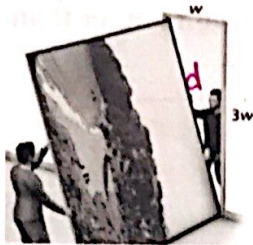
$$= 6 \sqrt{7 \cdot 7 \cdot 2 \cdot t^2 \cdot t}$$

$$= 6 \sqrt{49t^2} \sqrt{2t}$$

$$= 6 \cdot 7t \sqrt{2t} = \boxed{42t\sqrt{2t}}$$

- Writing a Radical Expression

- A rectangular door in a museum is three times as tall as it is wide. What is a simplified expression for the maximum length of a painting that fits through the door?



$$d^2 = w^2 + (3w)^2$$

$$d^2 = w^2 + 9w^2$$

$$d^2 = 10w^2$$

$$d = \sqrt{10w^2} = \sqrt{w^2} \sqrt{10}$$

$$\boxed{d = w\sqrt{10}}$$

- Simplifying Fractions within Radicals

- Division Property of Square Roots

- For $a \geq 0$ and $b > 0$, $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$

- When a radicand has a denominator that is a perfect square, it is easier to apply the division property of square roots first, and then simplify the numerator and denominator of the result.

- Ex: What is the simplified form of $\sqrt{\frac{64}{49}}$?

$$= \frac{\sqrt{64}}{\sqrt{49}} = \boxed{\frac{8}{7}}$$

- Ex: What is the simplified form of $\sqrt{\frac{8x^3}{50x}}$?

$$= \sqrt{\frac{4x^2}{25}} = \frac{\sqrt{4x^2}}{\sqrt{25}} = \boxed{\frac{2x}{5}}$$

- Rationalizing Denominators

- When a radicand in the denominator is not a perfect square, you may need to rationalize the denominator to remove the radical.

- Multiply both the numerator and the denominator by the same radical expression.

- Ex: What are the simplified forms of $\frac{\sqrt{3}}{\sqrt{7}}$ and $\frac{\sqrt{7}}{\sqrt{8n}}$?

$$\frac{\sqrt{3}}{\sqrt{7}} \cdot \frac{\sqrt{7}}{\sqrt{7}} = \boxed{\frac{\sqrt{21}}{7}}$$

$$\frac{\sqrt{7}}{\sqrt{8n}} \cdot \frac{\sqrt{8n}}{\sqrt{8n}} = \frac{\sqrt{56n}}{8n} = \frac{\sqrt{4 \cdot 14n}}{8n}$$

$$= \frac{2\sqrt{14n}}{8n} = \boxed{\frac{\sqrt{14n}}{4n}}$$

5.5 Rational Exponents and Radicals (M2 10.4)

Obj.: I will be able to convert between radical form and exponential form of powers with rational exponents. I will be able to apply radical expressions to real-world situations.

Finding Roots

You can use rational exponents to represent radicals.

In a radical expression, $\sqrt[n]{a}$,

• "a" is the radicand

• "n" is the index

○ Gives the degree of the root.

○ If no index is listed, it is assumed to be 2, meaning square root.

You can simplify radical expressions by finding like factors.

• Ex: What is the simplified form of each expression?

$$\sqrt[3]{125} = \sqrt[3]{5 \cdot 5 \cdot 5} = \boxed{5}$$

$$\sqrt[4]{16} = \sqrt[4]{2 \cdot 2 \cdot 2 \cdot 2} = \boxed{2}$$

Converting to Radical Form

You can also write expressions that have rational exponents, like $\frac{2}{3}$, in radical form.

• If the nth root of a is a real number, and m and n are positive integers, then

$$a^{\frac{1}{n}} = \sqrt[n]{a} \quad \text{and} \quad a^{\frac{m}{n}} = \sqrt[n]{a^m} = (\sqrt[n]{a})^m$$

• Ex: What is $12a^{\frac{2}{3}}$ in radical form?

$$= 12 \cdot \sqrt[3]{a^2}$$

↑ not part of radicand b/c not part of base

• Ex: What is $(64a)^{\frac{4}{5}}$ in radical form?

$$= (32 \cdot 2a)^{\frac{4}{5}}$$

$$= 32^{\frac{4}{5}} (2a)^{\frac{4}{5}}$$

$$= (2^5)^{\frac{4}{5}} (2a)^{\frac{4}{5}}$$

$$= 2^4 (2a)^{\frac{4}{5}} = 16 \sqrt[5]{(2a)^4}$$

Converting to Exponential Form

• Ex: What is $\sqrt[5]{b^3}$ in exponential form?

$$= \boxed{b^{3/5}}$$

• Ex: What is $\sqrt[3]{27d^5}$ in exponential form?

$$= (27d^5)^{1/3}$$

$$= 27^{1/3} d^{5/3} = \boxed{3d^{5/3}}$$

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• Using a Radical Expression

- You can estimate the metabolic rate of living organisms based on body mass using Kleiber's law. The formula $R = 73.3\sqrt[4]{M^3}$ relates metabolic rate R measured in Calories per day to body mass M measured in kilograms. What is the metabolic rate of a dog with a body mass of 18kg?

$$R = 73.3\sqrt[4]{M^3}$$

$$M = 18$$

$$R = 73.3 (M)^{3/4}$$
$$= 73.3 (18)^{3/4}$$

$$R = 640.6 \text{ calories/day}$$

- A company that manufactures memory chips for digital cameras uses the formula $c = 120\sqrt[3]{n^2} + 1300$ to determine the cost, c , in dollars, of producing n chips. How much will it cost to produce 250 chips?

$$C = 120n^{2/3} + 1300$$

$$n = 250$$

$$C = 120(250)^{2/3} + 1300$$

$$C = \$6062.20$$

- Carbon-14 is present in all living organisms and decays at a predictable rate. To estimate the age of an organism, archaeologists measure the amount of carbon-14 remaining after 5000 years can be found using the formula $A = A_0(2.7)^{-3/5}$, where A_0 is the initial amount of carbon-14 in the sample that is tested. How much carbon-14 is left in a 5000-year-old sample that originally contained 7.0×10^{-12} grams of carbon-14?

$$A = A_0 (2.7)^{-3/5}$$

$$A_0 = 7.0 \times 10^{-12}$$

$$A = (7.0 \times 10^{-12})(2.7)^{-3/5}$$

$$A = 3.9 \times 10^{-12} \text{ g}$$

5.6 Pythagorean Theorem, Midpoint & Distance (M1 7.6)

Obj.: I will be able to find the midpoint, endpoint, or distance of a line segment.

• Finding the Midpoint

- On a number line, the coordinate of the midpoint is the average (or mean) of the coordinates of the endpoints.

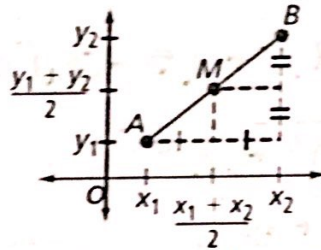


$$A = a$$

$$B = b$$

$$M = \frac{a+b}{2}$$

- In the coordinate plane, the coordinates of the midpoint are the average of the x-coordinates and the average of the y-coordinates of the endpoints.



$$A = (x_1, y_1)$$

$$B = (x_2, y_2)$$

$$M = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

- Ex: \overline{AB} has endpoints at -4 and 9. What is the coordinate of its midpoint?

$$\frac{-4+9}{2} = \boxed{\frac{5}{2}}$$

- Ex: \overline{EF} has endpoints $E(7,5)$ and $F(2,-4)$. What are the coordinates of its midpoint M?

$$\left(\frac{7+2}{2}, \frac{5+(-4)}{2} \right)$$

or

$$\frac{(7,5)}{2} + \frac{(2,-4)}{2} = \boxed{\left(\frac{9}{2}, \frac{1}{2} \right)}$$

$$= \boxed{\left(\frac{9}{2}, \frac{1}{2} \right)}$$

• Finding the Endpoint

- When you know the midpoint and the endpoint of a segment, you can use the Midpoint Formula to find the other endpoint.

- Ex: The midpoint of \overline{CD} is $M(-2,1)$. One endpoint is $C(-5,7)$. What are the coordinates of the other endpoint D?

$$-2 = \frac{-5+x}{2} \quad 1 = \frac{7+y}{2}$$

or

$$-4 = -5+x \quad 2 = 7+y$$

$$1 = x \quad -5 = y \quad \boxed{(1, -5)}$$

$$\frac{(-2, 1)}{2} \cdot 2$$

$$\frac{(-4, 2)}{2}$$

$$- \frac{(-5, 7)}{2}$$

- Ex: The midpoint of \overline{AB} has coordinates $(4, -9)$. Endpoint A has $(-3, -5)$. What are the coordinates of B?

$$4 = \frac{-3+x}{2} \quad -9 = \frac{-5+y}{2}$$

$$8 = -3+x \quad -18 = -5+y$$

$$11 = x \quad -13 = y$$

$$\boxed{(11, -13)}$$

or

$$(4, -9) \cdot 2$$

$$= (8, -18)$$

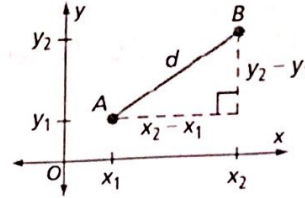
$$+ (+3, +5)$$

$$\boxed{(11, -13)}$$

• Finding Distance

- Recall that the Pythagorean Theorem states that for any right triangle with hypotenuse c and legs a and b , $a^2 + b^2 = c^2$.
- The distance between two points $A(x_1, y_1)$ and $B(x_2, y_2)$ is

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



- Ex: What is the distance between $U(-7, 5)$ and $V(4, -3)$? Round to the nearest tenth.

$$\begin{aligned} d &= \sqrt{(-7-4)^2 + (5-(-3))^2} \\ &= \sqrt{(-11)^2 + (8)^2} \\ &= \sqrt{121+64} \\ &= \sqrt{185} = 13.6 \end{aligned}$$

or

$$\begin{aligned} &(-7, 5) \\ &- (4, -3) \\ &\hline &(-11, 8)^2 \\ &(121+64) \\ &= \sqrt{185} = 13.6 \end{aligned}$$

- Ex: \overline{SR} has endpoints $S(-2, 14)$ and $R(3, -1)$. What is SR to the nearest tenth?

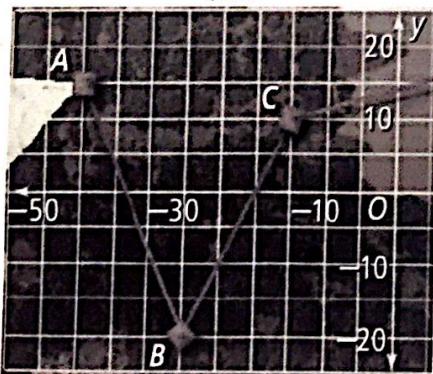
$$\begin{aligned} d &= \sqrt{(-2-3)^2 + (14-(-1))^2} \\ &= \sqrt{(-5)^2 + (15)^2} \\ &= \sqrt{25+225} \\ &= \sqrt{250} = 15.8 \end{aligned}$$

or

$$\begin{aligned} &(-2, 14) \\ &- (3, -1) \\ &\hline &(-5, 15)^2 \\ &25+225 \\ &= \sqrt{250} \\ &= 15.8 \end{aligned}$$

• Applying Distance

- On a zip-line course, you are harnessed to a cable that travels through the treetops. You start at Platform A and zip to each of the other platforms. How far did you travel from Platform B to Platform C? Each grid unit represents 5m.



$B(-30, -20)$
 $C(-15, 10)$

$$\begin{aligned} d &= \sqrt{(-30-(-15))^2 + (-20-10)^2} \\ &= \sqrt{(-15)^2 + (-30)^2} \\ &= \sqrt{225+900} \\ &= \sqrt{1125} \\ &= \sqrt{225} \sqrt{5} \\ &= 15\sqrt{5} \\ &= 33.5 \end{aligned}$$

$$\begin{aligned} &(-30, -20) \\ &- (-15, 10) \\ &\hline &(-15, -30)^2 \\ &225+900 \\ &= 1125 \\ &= \sqrt{1125} \\ &= 33.5 \end{aligned}$$

5.7 Square Root Equations (M3 6.5)

Obj.: I will be able to use properties of radicals to solve simple radical equations.

- Solving a Square Root Equation

- A radical equation is an equation that has a variable in the radicand or a variable with a rational exponent.
- If the radical has index 2, the equation is a square root equation.
- To solve a radical equation, isolate - the radical on one side of the equation. Then raise each side to the power suggested by the index.

- Ex: What is the solution of $3 + \sqrt{2x - 3} = 8$?

$$\begin{array}{r} 3 + \sqrt{2x - 3} = 8 \\ -3 \quad -3 \end{array}$$

$$\begin{array}{r} 2x + (-3) = 25 \\ +3 \quad +3 \end{array}$$

$$(\sqrt{2x - 3} = 5)^2$$

$$2x = 28$$

$$\boxed{x = 14}$$

- Ex: What is the solution of $3\sqrt{x} + 3 = 15$?

$$\begin{array}{r} 3\sqrt{x} + 3 = 15 \\ -3 \quad -3 \end{array}$$

$$\frac{3\sqrt{x}}{3} = \frac{12}{3}$$

$$(\sqrt{x} = 4)^2$$

$$\boxed{x = 16}$$

- Ex: What is the solution of $(\sqrt{4x + 1} = 5)^2$?

$$4x + 1 = 25$$

$$4x = 24$$

$$\boxed{x = 6}$$

- Ex: What is the solution of $\sqrt{2x + 3} - 7 = 0$?

$$\begin{array}{r} \sqrt{2x + 3} - 7 = 0 \\ +7 \quad +7 \end{array}$$

$$(\sqrt{2x + 3} = 7)^2$$

$$2x + 3 = 49$$

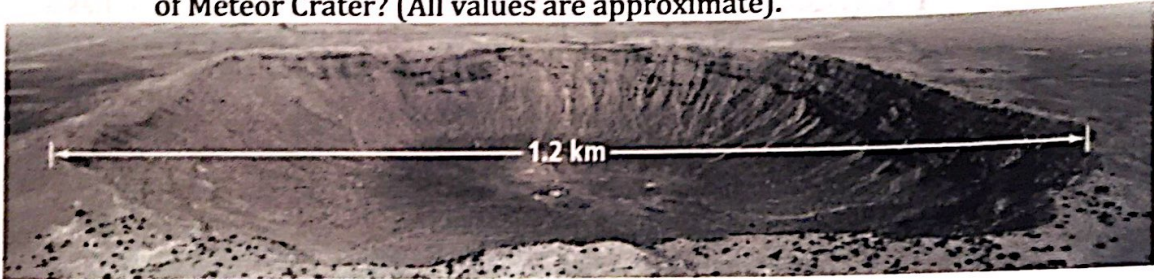
$$2x = 46$$

$$\boxed{x = 23}$$

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• Using Radical Equations

- For Meteor Crater in Arizona, the formula $d = 2 \sqrt[3]{\frac{V}{0.3}}$ relates the diameter d of the rim (in meters) to the volume V (in cubic meters). What is the volume of Meteor Crater? (All values are approximate).



$$d = 1.2 \text{ km} \\ = 1200 \text{ m}$$

$$\frac{1200}{2} = \frac{2 \sqrt[3]{\frac{V}{0.3}}}{2} \\ \left(600 = \sqrt[3]{\frac{V}{0.3}} \right)^3$$

$$2.16 \cdot 10^8 = \frac{V}{0.3}$$

$$\boxed{6.48 \cdot 10^7 = V}$$

- The formula $\frac{\pi d^2 v}{4} = Q$ models the diameter of a pipe where Q is the maximum flow of water in a pipe, and v is the velocity of the water. What is the diameter of a pipe that allows a maximum flow of $30 \text{ ft}^3/\text{min}$ of water flowing at a velocity of $400 \text{ ft}/\text{min}$? Round your answers to the nearest inch.

$$Q = 30 \frac{\text{ft}^3}{\text{min}}$$

$$v = 400 \text{ ft}/\text{min}$$

$$d = ?$$

$$\frac{\pi d^2 (400)}{4} = 30$$

$$\frac{100 \pi d^2}{100 \pi} = \frac{30}{100 \pi}$$

$$\sqrt{d^2} = \sqrt{\frac{30}{100 \pi}}$$

$$d = \sqrt{\frac{30}{100 \pi}}$$

$$d = 0.09549 \text{ ft} \times \frac{12 \text{ in}}{1 \text{ ft}}$$

$$\boxed{d = 1 \text{ in}}$$